CS 242

## **Types**

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## Type

A type is a collection of computable values that share some structural property.

- Examples
  - p103
  - IntegersStrings
  - int  $\rightarrow$  bool
  - (int → int) →bool
- "Non-examples"
  - {3, true, λx.x}
  - · Even integers
  - $\{f: int \rightarrow int \mid if x>3$ then  $f(x) > x^*(x+1)\}$

Distinction between types and non-types is language dependent.

## Uses for types

- Program organization and documentation
  - Separate types for separate concepts
    - Represent concepts from problem domain
  - Indicate intended use of declared identifiers

     Types can be checked, unlike program comments
- Identify and prevent errors
  - Compile-time or run-time checking can prevent meaningless computations such as 3 + true - "Bill"
- Support optimization
  - · Example: short integers require fewer bits
  - · Access record component by known offset

## Type errors

- Hardware error
  - function call x() where x is not a function
  - may cause jump to instruction that does not contain a legal op code
- Unintended semantics
  - int\_add(3, 4.5)
  - not a hardware error, since bit pattern of float 4.5 can be interpreted as an integer
  - just as much an error as x() above

## General definition of type error

- ◆ A *type error* occurs when execution of program is not faithful to the intended semantics
- ◆Do you like this definition?
  - Store 4.5 in memory as a floating-point number
     Location contains a particular bit pattern
  - To interpret bit pattern, we need to know the type
  - If we pass bit pattern to integer addition function, the pattern will be interpreted as an integer pattern
     Type error if the pattern was intended to represent 4.5

## Compile-time vs run-time checking

- ◆Lisp uses run-time type checking
  - (car x) check first to make sure x is list
- ◆ML uses compile-time type checking
  - f(x) must have  $f: A \rightarrow B$  and x: A
- ◆Basic tradeoff
  - · Both prevent type errors
  - · Run-time checking slows down execution
  - Compile-time checking restricts program flexibility Lisp list: elements can have different types ML list: all elements must have same type

## **Expressiveness**

In Lisp, we can write function like

(lambda (x) (cond ((less x 10) x) (T (car x)))) Some uses will produce type error, some will not

Static typing always conservative

if (big-hairy -boolean-expression) then ((lambda (x) ... ) 5) else ((lambda (x) ... ) 10)

Cannot decide at compile time if run-time error will occur

## Relative type-safety of languages

- ◆Not safe: BCPL family, including C and C++
  - · Casts, pointer arithmetic
- Almost safe: Algol family, Pascal, Ada.
  - · Dangling pointers.
    - Allocate a pointer p to an integer, deallocate the memory referenced by p, then later use the value pointed to by p
    - No language with explicit deallocation of memory is fully
- ◆Safe: Lisp, ML, Smalltalk, and Java
  - · Lisp, Smalltalk: dynamically typed
  - ML, Java: statically typed

## Type checking and type inference

Standard type checking

int f(int x) { return x+1; }; int g(int y) { return f(y+1)\*2; };

- · Look at body of each function and use declared types of identifies to check agreement.
- ◆Type inference

Mf(i)Kx) { return x+1; };  $\not\bowtie$  g( $\not\bowtie$  y) { return f(y+1)\*2;};

· Look at code without type information and figure out what types could have been declared.

ML is designed to make type inference tractable.

## ML Type Inference

Example

- fun f(x) = 2 + x;

> val it = fn : int  $\rightarrow$  int

- ◆How does this work?
  - + has two types:  $int*int \rightarrow int$ , real\*real $\rightarrow$ real
  - 2 : int has only one type
  - This implies + : int\* int → int
  - From context, need x: int
  - Therefore f(x:int) = 2+x has type  $int \rightarrow int$

Overloaded + is unusual. Most ML symbols have unique type. In many cases, unique type may be polymorphic.

## Another presentation

### **◆**Example

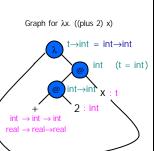
- fun f(x) = 2+x; > val it = fn : int  $\rightarrow$  int

◆How does this work? Assign types to leaves

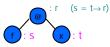
Propagate to internal nodes and generate

constraints

Solve by substitution

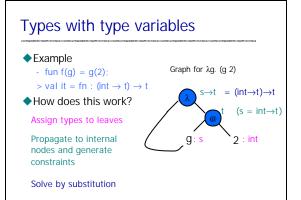


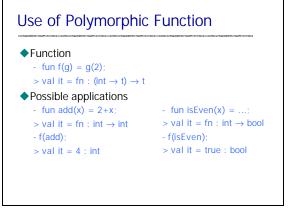
## Application and Abstraction



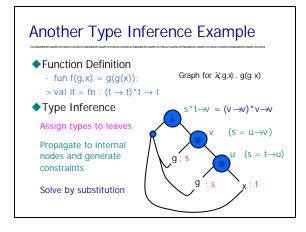


- Application
  - · f must have function type domain→ range
  - domain of f must be type of argument x
  - · result type is range of f
- Function expression
  - Type is function type
  - domain→ range · Domain is type of variable x
  - · Range is type of function body e

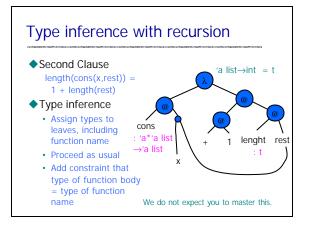




## Recognizing type errors Function - fun f(g) = g(2); > val it = fn : (int $\rightarrow$ t) $\rightarrow$ t Incorrect use - fun not(x) = if x then false else true; > val it = fn : bool $\rightarrow$ bool - f(not); Type error: cannot make bool $\rightarrow$ bool = int $\rightarrow$ t



# Polymorphic Datatypes Datatype with type variable 'a is syntax for \*type variable a\* datatype 'a list = nil | cons of 'a\* ('a list) nil: 'a list cons: 'a\* ('a list) → 'a list Polymorphic function fun length nil = 0 length (cons(x,rest)) = 1 + length(rest) length: 'a list → int Type inference Infer separate type for each clause Combine by making two types equal (if necessary)



## Main Points about Type Inference

- ◆Compute type of expression
  - Does not require type declarations for variables
  - Find most general type by solving constraints
  - · Leads to polymorphism
- ◆ Static type checking without type specifications
- May lead to better error detection than ordinary type checking
  - Type may indicate a programming error even if there is no type error (example following slide).

## Information from type inference

◆An interesting function on lists

```
fun reverse (nil) = nil
| reverse (x::lst) = reverse(lst);
```

◆Most general type

reverse : 'a list  $\rightarrow$  'b list

What does this mean?
Since reversing a list does not change its type, there must be an error in the definition of

rovorce

## Compare C++ templates

- ◆Sec 6.4.1 Parametric polymorphism
- ◆Sec 6.4.2 Implementation of parametric poly

## Polymorphism vs Overloading

- ◆Parametric polymorphism
  - Single algorithm may be given many types
  - Type variable may be replaced by any type
  - $f: t \rightarrow t => f: int \rightarrow int, f: bool \rightarrow bool, ...$
- Overloading
  - · A single symbol may refer to more than one algorithm
  - · Each algorithm may have different type
  - Choice of algorithm determined by type context
  - Types of symbol may be arbitrarily different
  - + has types int\*int→int, real\*real→real, no others

## Parametric Polymorphism: ML vs C++

- ◆ML polymorphic function
  - Declaration has no type information
  - Type inference: type expression with variables
  - Type inference: substitute for variables as needed
- ◆C++ function template
  - Declaration gives type of function arg, result
  - Place inside template to define type variables
  - Function application: type checker does instantiation

ML also has module system with explicit type parameters

## Example: swap two values

```
    fun swap(x,y) =
        let val z = !x in x := !y; y := z end;
val swap = fn : 'a ref * 'a ref -> unit
```

◆C++ template <typ

template < typename T >
void swap(T&, T& y) {
 T tmp = x; x=y; y=tmp;
}

Declarations look similar, but compiled is very differently

## **Implementation**

- ML
  - Swap is compiled into one function
  - Typechecker determines how function can be used
- ◆C++
  - Swap is compiled into linkable format
  - Linker duplicates code for each type of use
- ◆Why the difference?
  - ML ref cell is passed by pointer, local x is pointer to value on heap
  - C++ arguments passed by reference (pointer), but local x is on stack, size depends on type

## Another example

◆C++ polymorphic sort function

```
template <typename T>
void sort( int count, T *A[count] ) {
  for (int i=0; i<count-1; i++)
     for (int j=i+1; j<count-1; j++)
          if (A[j] < A[i]) swap(A[i],A[j]);
}</pre>
```

- ♦ What parts of implementation depend on type?
  - Indexing into array
  - Meaning and implementation of <

## **ML** Overloading

- Some predefined operators are overloaded
- ◆User-defined functions must have unique type
  - fun plus(x,y) = x+y;
  - > Error: overloaded variable cannot be resolved: +
- ◆Why is a unique type needed?
  - Need to compile code  $\Rightarrow$  need to know which +
  - · Efficiency of type inference
  - Aside: General overloading is NP-complete Two types, true and false Overloaded functions

and : {true\*true→true, false\*true→false, ...}

## Main Points about ML

- ◆General-purpose procedural language
  - We have looked at "core language" only
  - Also: abstract data types, modules, concurrency,....
- ◆Well-designed type system
  - Type inference
  - Polymorphism
  - Reliable -- no loopholes
  - · Limited overloading