## The Algol Family and ML

John Mitchell

## Algol 60

Basic Language of 1960

- Simple imperative language + functions
- Successful syntax, BNF -- used by many successors
- statement oriented
- Begin ... End blocks (like C \{ ... \} )
- if ... then ... else
- Recursive functions and stack storage allocation
- Fewer ad hoc restrictions than Fortran - General array references: $A[x+B[3] * y]$
- Type discipline was improved by later languages
- Very influential but not widely used in US


## Language Sequence



Many other languages:
Algol 58, Algol W, Euclid, EL1, Mesa (PARC), ...
Modula-2, Oberon, Modula-3 (DEC)

## Algol 60 Sample

real procedure average (A,n); real array $A$; integer $n$; $\quad$ no array bounds begin
real sum; sum :=0;
for $\mathrm{i}=1$ step 1 until n do sum := sum $+A[i]$;
average := sum/n $\qquad$ no ; here end;

set procedure return value by assignment

## Algol Joke

Question

- Is $x:=x$ equivalent to doing nothing?
- Interesting answer in Algol
integer procedure $p$;
begin

$$
p:=p
$$

end;

- Assignment here is actually a recursive call


## Some trouble spots in Algol 60

Type discipline improved by later languages

- parameter types can be array

> - no array bounds

- parameter type can be procedure
- no argument or return types for procedure parameter
- Parameter passing methods
- Pass-by-name had various anomalies
- "Copy rule" based on substitution, interacts with side effects
- Pass-by-value expensive for arrays

Some awkward control issues

- goto out of block requires memory management


## Algol 60 Pass-by-name

-Substitute text of actual parameter

- Unpredictable with side effects!


## - Example

procedure inc2(i, j);
integer i, j;
begin
begin
$\mathrm{i}:=\mathrm{i}+1$;
$\mathrm{k}:=\mathrm{k}+1$;
$j:=j+1$
end;
inc2 (k, A[k]);
Is this what you expected?

## Algol 68

Considered difficult to understand

- Idiosyncratic terminology
- types were called "modes"
- arrays were called "multiple values"
- $v$ W grammars instead of BNF
- context-sensitive grammar invented by A. van Wijngaarden
- Elaborate type system
- Complicated type conversions
- Fixed some problems of Algol 60
- Eliminated pass-by-name
- Not widely adopted


## Algol 68 Modes

Primitive modes

- int
- real
- char
- bool
- string
- compl (complex)
- bits
- bytes
- sema (semaphore)
- format (I/O)
- file

Compound modes

- arrays
- structures
- procedures
- sets
- pointers

Rich and structured type system is a major contribution of Algol 68

## Other features of Algol 68

Storage management

- Local storage on stack
- Heap storage, explicit alloc and garbage collection
- Parameter passing
- Pass-by-value
- Use pointer types to obtain Pass-by-reference
- Assignable procedure variables
- Follow "orthogonality " principle rigorously


## Pascal

## Limitations of Pascal

- Array bounds part of type
procedure p(a: array [1..10] of integer)
procedure $p(n$ : integer, a : array [1. n]) of integer)
- Attempt at orthogonal design backfires
- parameter must be given a type
- type cannot contain variables

How could this have happened? Emphasis on teaching

- Not successful for "industrial-strength" projects
- Kernighan -- Why Pascal is not my favorite language
- Left niche for C ; niche has expanded!!


## ML

Typed programming language

- Intended for interactive use

Combination of Lisp and Algol-like features

- Expression-oriented
- Higher-order functions
- Garbage collection
- Abstract data types
- Module system
- Exceptions
- General purpose non-C-like, not 00 language


## Goals in study of ML

-Survey a modern procedural language
-Discuss general programming languages issues

- Types and type checking
- General issues in static/dynamic typing
- Type inference
- Polymorphism and Generic Programming
- Memory management
- Static scope and block structure
- Function activation records, higher-order functions
- Control
- Force and delay
- Exceptions
- Tail recursion and continuations


## History of ML



Robin Milner
Logic for Computable Functions

- Stanford 1970-71
- Edinburgh 1972-1995
- Meta-Language of the LCF system
- Theorem proving
- Type system
- Higher-order functions


## Logic for Computable Functions

-Dana Scott, 1969

- Formulate logic for proving properties of typed functional programs
- Milner
- Project to automate logic
- Notation for programs
- Notation for assertions and proofs
- Need to write programs that find proofs
- Too much work to construct full formal proof by hand
- Make sure proofs are correct


## LCF proof search

Tactic: function that tries to find proof
tactic(formula $)=\left\{\begin{array}{l}\text { succeed and return proof } \\ \text { search forever } \\ \text { fail }\end{array}\right.$

- Express tactics in the Meta-Language (ML)
-Use type system to facilitate correctness


## Tactics in ML type system

- Tactic has a functional type
tactic : formula $\rightarrow$ proof
- Type system must allow "failure"
tactic(formula) $=\left\{\begin{array}{l}\text { succeed and return proof } \\ \text { search forever } \\ \text { fail and raise exception }\end{array}\right.$


## Function types in ML

$f: A \rightarrow B$ means
for every $x \in A$,
$f(x)=\left\{\begin{array}{l}\text { some element } y=f(x) \in B \\ \text { run forever } \\ \text { terminate by raising an exception }\end{array}\right.$

In words, "if $f(x)$ terminates normally, then $f(x) \in B$." Addition never occurs in $f(x)+3$ if $f(x)$ raises exception.

This form of function type arises directly from motivating application for ML. Integration of type system and exception mechanism mentioned in Milner's 1991 Turing Award.

## Higher-Order Functions

Tactic is a function

- Method for combining tactics is a function on functions
- Example:
$\mathrm{f}\left(\right.$ tactic $_{1}$, tactic $\left._{2}\right)=$
$\lambda$ formula. try tactic ${ }_{1}$ (formula) else tactic ${ }_{2}$ (formula)


## Basic Overview of ML

- Interactive compiler: read-eval-print
- Compiler infers type before compiling or executing Type system does not allow casts or other loopholes.
- Examples
$-(5+3)-2$;
$>$ val it $=6$ : int
- if $5>3$ then "Bob" else "Fido";
> val it = "Bob" : string
- $5=4$;
$>$ val it = false : bool


## Overview by Type

## Booleans

- true, false : bool
- if ... then ... else ... (types must match)
- Integers
- $0,1,2, \ldots$ : int
- $+, *, \ldots$ : int $*$ int $\rightarrow$ int and so on ...

Strings

- "Austin Powers"


## - Reals

- $1.0,2.2,3.14159, \ldots$ decimal point used to disambiguate


## Compound Types

Tuples

- (4, 5, "noxious") : int * int * string
- Lists
- nil
- 1 :: $[2,3,4]$ infix cons notation


## - Records

- $\{$ name $=$ "Fido", hungry=true $\}$
: \{name: string, hungry : bool\}


## Patterns and Declarations

Patterns can be used in place of variables
<pat> ::= <var> | <tuple> | <cons> | <record> ..

- Value declarations
- General form
val <pat> = <exp>
- Examples
val myTuple = ("Conrad", "Lorenz");
val ( $\mathrm{x}, \mathrm{y}$ ) = myTuple;
val myList $=[1,2,3,4]$;
val $x:$ :rest $=$ myList,
- Local declarations
let val $x=2+3$ in $x^{*} 4$ end;


## Functions and Pattern Matching

-Anonymous function

- $\mathrm{fn} \mathrm{x}=>\mathrm{x}+1$; like Lisp lambda
- Declaration form
- fun <name> <pat ${ }_{1}>=<\exp _{1}>$
| <name> <pat ${ }_{2}>=<\exp _{2}>\ldots$
| <name> <pat $>=<\exp _{n}>\ldots$
- Examples
- fun $f(x, y)=x+y ; \quad$ actual par must match pattern $(x, y)$
- fun length nil $=0$
| length (x::s) $=1+$ length(s);


## More functions on lists

Reverse a list
fun reverse nil $=$ nil
| reverse (x::xs) = append ((reverse xs), [x]);

- Append lists
fun append(nil, ys) $=y s$
| append(x::xs, ys) = x:: append(xs, ys);
Questions
- How efficient is reverse?
- Can you do this with only one pass through list?


## Datatype Declarations

General form
datatype <name> = <clause> | ... $\mid$ <clause>
<clause> ::= <constructor> |<contructor> of <type>

## - Examples

- datatype color = red | yellow | blue - elements are red, yellow, blue
- datatype atom $=$ atm of string $\mid$ nmbr of int - elements are $\operatorname{atm}\left({ }^{\prime \prime} A^{\prime}\right), \operatorname{atm}\left({ }^{\prime \prime} B^{\prime \prime}\right), \ldots, n m b r(0), n m b r(1), \ldots$
- datatype list $=$ nil | cons of atom*list - elements are nil, cons(atm("A"), nil), ... cons(nmbr(2), cons(atm("ugh"), nil)), ...


## Map function on lists

- Apply function to every element of list


## fun map (f, nil) = nil

| $\operatorname{map}(f, x:: x s)=f(x):: \operatorname{map}(f, x s)$; $\operatorname{map}(\mathrm{fn} x=>\mathrm{x}+1,[1,2,3]) ; \quad[2,3,4]$

## -Compare to Lisp

(define map
(lambda (f xs) (if (eq? xs ()) () (cons (f (car xs)) (map f (cdr xs))) )))

## More efficient reverse function

fun reverse xs = let fun rev $($ nil, $z)=($ nil, $z)$ | $\operatorname{rev}(y:: y s, z)=\operatorname{rev}(y s, y:: z)$ val $(u, v)=\operatorname{rev}(x s, n i l)$
in $v$
end;


## Datatype and pattern matching

Recursively defined data structure
datatype tree = leaf of int $\mid$ node of int*tree*tree
node(4, node(3,leaf(1), leaf(2)), node(5,leaf(6), leaf(7))

```
        )
```

- Recursive function

fun sum (leaf $n$ ) $=n$
\| $\operatorname{sum}(\operatorname{node}(n, t 1, t 2))=n+\operatorname{sum}(t 1)+\operatorname{sum}(t 2)$


## Example: Evaluating Expressions

- Define datatype of expressions
datatype exp $=$ Var of int | Const of int | Plus of exp* exp; Write $(x+3)+y$ as Plus(Plus(Var(1),Const(3)), $\operatorname{Var}(2))$
- Evaluation function
fun $\operatorname{ev}(\operatorname{Var}(n))=\operatorname{Var}(n)$
| ev(Const(n)) $=$ Const( $n$ )
| ev(Plus(e1,e2)) = ...
Examples
$\mathrm{ev}($ Plus(Const(3),Const(2))) $\Rightarrow$ Const(5)
ev(Plus(Var(1),Plus(Const(2),Const(3))))
$\Longrightarrow \quad \mathrm{ev}(\operatorname{Plus}(\operatorname{Var}(1)$, Const(5))


## Evaluation by cases

## Variables and assignment

-General terminology: L-values and R-values

- Assignment $y:=x+3$
- Identifier on left refers to a memory location, called $L$-value
- Identifier on right refers to contents, called R-value


## - Variables

- Basic properties
- A variable names a storage location
- Contents of location can be read, can be changed
- ML
- A variable is another type of value
- Explicit operations to read contents or change contents
- Separates naming (declaration of identifiers) from "variables"

```
datatype exp = Var of int | Const of int | Plus of exp* exp;
```

datatype exp = Var of int | Const of int | Plus of exp* exp;
fun ev(Var(n)) = Var(n)
fun ev(Var(n)) = Var(n)
| ev(Const(n)) = Const(n)
| ev(Const(n)) = Const(n)
| ev(Plus(e1,e2)) = (case ev(e1) of
| ev(Plus(e1,e2)) = (case ev(e1) of
Var(n) => Plus(Var(n),ev(e2)) |
Var(n) => Plus(Var(n),ev(e2)) |
Const(n) => (case ev(e2) of
Const(n) => (case ev(e2) of
Var(m) => Plus(Const(n),Var(m )) |
Var(m) => Plus(Const(n),Var(m )) |
Const(m) => Const(n+m)
Const(m) => Const(n+m)
Plus(e3,e4) => Plus(Const(n),Plus(e3,e4)) ) |
Plus(e3,e4) => Plus(Const(n),Plus(e3,e4)) ) |
Plus(e3,e4) => Plus(Plus(e3,e4),ev(e2)) );
Plus(e3,e4) => Plus(Plus(e3,e4),ev(e2)) );
|

```
        |
```


## Case expression

Datatype
datatype exp = Var of int | Const of int | Plus of exp* exp;

- Case expression

```
case e of
```

$\operatorname{Var}(\mathrm{n})=>. . \mid$
Const(n) => .... |
Plus(e1,e2) => ...

## Core ML

## Basic Types

- Unit
- Booleans
- Integers
- Strings
- Reals
- Tuples $\quad$ Type declarations
- Lists
- Records
- Exceptions
- Reference Cells


## ML imperative constructs

ML reference cells

- Different types for location and contents
$x$ : int non-assignable integer value
$y$ : int ref location whose contents must be integer
!y the contents of location $y$
ref x expression creating new cell initialized to x
- ML assignment
operator := applied to memory cell and new contents
- Examples
$y:=x+3$ place value of $x+3$ in cell $y$; requires $x$ int
$\mathrm{y}:=!\mathrm{y}+3$ add 3 to contents of y and store in location y


## ML examples

Create cell and change contents
val $x=$ ref "Bob";
$x:=$ "Bill";
Create cell and increment
val $y=$ ref 0 ;
$y:=!y+1 ;$
-While loop
val i = ref 0;
while $!i<10$ do $\mathrm{i}:=!\mathrm{i}+1$;
! i;

